

# Numerical benchmark campaign of COST Action TU1404 – microstructural modelling

## Supplementary material

### Model 4 - Micromechanical analytical model

Mateusz Wyrzykowski<sup>1</sup>, Julien Sanahuja<sup>2</sup>, Laurent Charpin<sup>2</sup>, Markus Königsberger<sup>3</sup>, Christian Hellmich<sup>3</sup>, Bernhard Pichler<sup>3</sup>, Luca Valentini<sup>4</sup>, Túlio Honório<sup>5\*</sup>, Vit Smilauer<sup>6</sup>, Karolina Hajkova<sup>6</sup>, Guang Ye<sup>7</sup>, Peng Gao<sup>7</sup>, Cyrille Dunant<sup>8</sup>, Adrien Hilaire<sup>9</sup>, Shashank Bishnoi<sup>10</sup>, Miguel Azenha<sup>11</sup>

<sup>1</sup> Empa, Swiss Federal Laboratories for Materials Science and Technology, Switzerland

<sup>2</sup> EDF, R&D MMC, France

<sup>3</sup> TU Wien, Austria

<sup>4</sup> University of Padua, Italy

<sup>5</sup> Université Paris-Est, Laboratoire Navier (UMR 8205), CNRS, ENPC, IFSTTAR, France

<sup>6</sup> Czech Technical University in Prague, Czech Republic

<sup>7</sup> TU Delft, The Netherlands

<sup>8</sup> Department of Engineering, University of Cambridge, UK

<sup>9</sup> EPFL, Lausanne, Switzerland

<sup>10</sup> IIT Delhi, India

<sup>11</sup> ISISE, University of Minho, Portugal

Received: 5 December 2017 / Accepted: 25 December 2017 / Published online: 30 December 2017

© The Author(s) 2017. This article is published with open access and licensed under a Creative Commons Attribution 4.0 International License.

---

## 1 Introduction

In this document the input data for model 4 - *micromechanical analytical model* used in the numerical benchmark [1] is presented as a supplementary material.

## 2 Input data - model 4

PSD was explicitly taken into account in the scenario following hydration kinetics model presented in [2].

From the oxide composition of cement provided, the contents of clinker minerals are obtained through Bogue equations.

Hydration balance equation of Tennis and Jennings [3] are used to represent hydration product assembly.

The multiscale nature of cement-based materials is depicted in the Figure 1.

The elastic properties of the phases at the cement paste scale are given in the Table 1.

---

\* Corresponding author (this supplementary material): Túlio Honório, E-mail: [tulio.honorio-de-faria@enpc.fr](mailto:tulio.honorio-de-faria@enpc.fr)

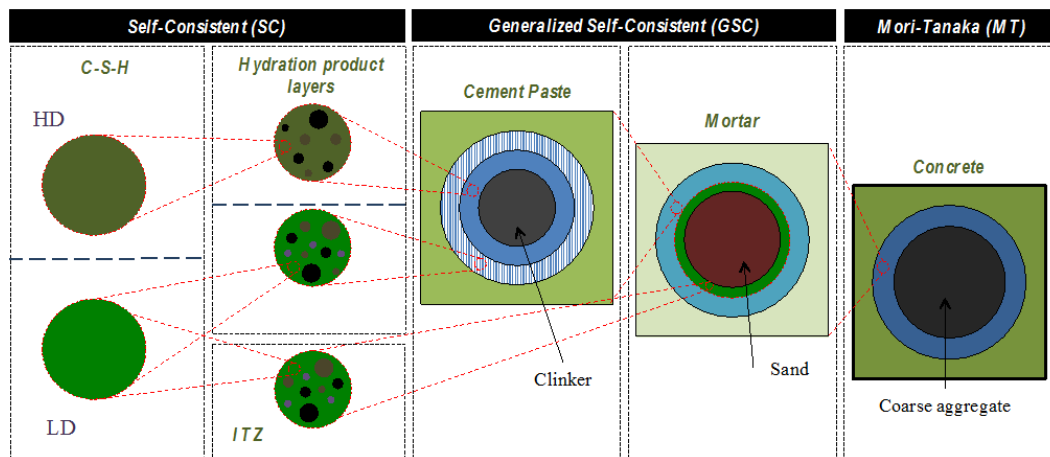


Figure 1 Representation of the multiscale nature of cement-based materials as in [4].

Table 1 Elastic properties of the different phases as in [5].

	Clinker	C-S-H			AFt	AFm	C <sub>3</sub> (A,F)H <sub>6</sub>	C <sub>4</sub> AH <sub>13</sub>	Gypsum	Sand
		LD	HD	CH						
E [GPa]	140	21.7	29.4	38	22.4	42.3	22.4	25	45.7	74.5
v	0.3	0.24	0.24	0.305	0.25	0.324	0.25	0.25	0.33	0.2
Ref.	[6]	[7]	[7]	[8]	[9]	[9]	[10]	[10]	[10]	[11]

## References

- [1] M. Wyrzykowski, et al., Numerical benchmark campaign of COST Action TU1404 – microstructural modelling. RILEM Technical Letters (2017) 2: 99-107. <http://dx.doi.org/10.21809/rilemtechlett.2017.44>
- [2] T. Honorio, B. Bary, F. Benboudjema, S. Poyet, Modeling hydration kinetics based on boundary nucleation and space-filling growth in a fixed confined zone. Cem Concr Res (2016) 83: 31-44. <https://doi.org/10.1016/j.cemconres.2016.01.012>
- [3] P.D. Tennis, H.M. Jennings, A model for two types of calcium silicate hydrate in the microstructure of Portland cement pastes. Cem Concr Res (2000) 30: 855-863. [https://doi.org/10.1016/S0008-8846\(00\)00257-X](https://doi.org/10.1016/S0008-8846(00)00257-X)
- [4] T. Honorio, B. Bary, F. Benboudjema, Thermal properties of cement-based materials: multiscale estimations at early-age. Cem Concr Compos (2017, submitted).
- [5] T. Honorio, B. Bary, F. Benboudjema, Multiscale estimation of ageing viscoelastic properties of cement-based materials: A combined analytical and numerical approach to estimate the behaviour at early age. Cem Concr Res (2016) 85: 137-155. <https://doi.org/10.1016/j.cemconres.2016.03.010>
- [6] K. Velez, et al., Determination by nanoindentation of elastic modulus and hardness of pure constituents of Portland cement clinker. Cem Concr Res (2001) 31: 555-561. [https://doi.org/10.1016/S0008-8846\(00\)00505-6](https://doi.org/10.1016/S0008-8846(00)00505-6)
- [7] O. Bernard, F.-J. Ulm, E. Lemarchand, A multiscale micromechanics-hydration model for the early-age elastic properties of cement-based materials. Cem Concr Res (2003) 33: 1293-1309. [https://doi.org/10.1016/S0008-8846\(03\)00039-5](https://doi.org/10.1016/S0008-8846(03)00039-5)
- [8] P.J.M. Monteiro, C.T. Chang, The elastic moduli of calcium hydroxide. Cem Concr Res (1995) 25: 1605-1609. [https://doi.org/10.1016/0008-8846\(95\)00154-9](https://doi.org/10.1016/0008-8846(95)00154-9)
- [9] S. Kamali, Comportement et simulation des matériaux cimentaires en environnement agressifs: lixiviation et température. Cachan, Ecole normale supérieure, 2003.
- [10] C.J. Haecker, et al., Modeling the linear elastic properties of Portland cement paste. Cem Concr Res (2005) 35: 1948-1960. <https://doi.org/10.1016/j.cemconres.2005.05.001>
- [11] E. Stora, Multi-scale modelling and simulations of the chemo-mechanical behavior of degraded cement-based materials. Université Paris-Est, 2007.