The kinetic competition between transport and oxidation of ferrous ions governs precipitation of corrosion products in carbonated concrete

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Abstract

Corrosion products, originating from steel corrosion in carbonated concrete and precipitating in the concrete pore system, can lead to cracking and spalling of the concrete cover. To avoid this common form of structural deterioration and thus ensure durable structures, reliable quantitative models are needed. Here, we present a new conceptual model to describe the fate of ferrous ions that are released at the steel surface during the corrosion process. The key novelty can be found in explicitly considering the kinetics of oxidation and transport of Fe^{2+} in the pore solution. These two processes constantly dilute the Fe^{2+} concentration and are in competition with the supply of Fe^{2+} from the anodic iron dissolution reaction. We use a numerical model to elucidate which of the described processes is the fastest. The results find good agreement with experimental data and reveal that under natural corrosion conditions, Fe^{2+} hardly reaches the saturation level, which permits the diffusion of corrosion products up to millimetres away from the steel without necessarily leading to expansive stresses. Under accelerated corrosion conditions, however, in a chloride-free environment, precipitation is accelerated immediately at the steel surface. This changes the corrosion products precipitation distribution and suggests careful evaluation of accelerated tests and related models.

Keywords: Diffusion; Iron solubility; Accelerated corrosion; Steel-concrete interface

1 Introduction

Reinforced concrete structures undergo a variety of degradation processes, among which corrosion-induced damages are the most common cause of deterioration [1, 2]. Therefore, the prediction of the event of corrosion induced concrete cover cracking due to precipitation of corrosion products is of key importance in service life prediction and structural design [3, 4]. The phenomenon has been studied and modeled through a variety of approaches. The laboratory experimentation of such process is limited by the very long time that it takes, for natural corrosion process, to get to such an advanced state, leading to the concrete cover cracking. That is why the process is generally accelerated by impressed current methods, which enhances the corrosion rate of steel embedded in concrete [5-10], and therefore enhances the formation of corrosion products. On the other hand, the process has been extensively modeled using a variety of approaches and computing techniques. The deterioration depends on the type of corrosion mechanism,

that is, corrosion being of uniform (carbonation induced) or localized (chloride induced) morphology [11]. Modeling studies typically considered corrosion induced cracking as a consequence of a uniform volume expansion of the steel rebar, which arises from the uniform formation of corrosion products on the steel surface, building up pressure against the concrete surrounding the steel [3, 5, 7, 12-16]. This assumption of a uniform volume expansion is certainly a strong simplification, as it has been experimentally found that, even in case of uniform corrosion, the formation of corrosion products can be non-uniformly distributed in the concrete matrix [5]. Nevertheless, a common model approach is to introduce a so-called "corrosion accommodation region" [5, 12] which is thought to be a porous cement paste layer around the steel bar, into which corrosion products can be pushed and no pressure is assumed to be exerted to the concrete until this porous zone is filled [7, 13, 16]. This concept allows to empirically model the time delay between the first release of corrosion

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products and the beginning of pressure build up, which is typically observed in experimental studies.

Modeling approaches consider instantaneous precipitation of corrosion products quantified by Faraday's law [3]. This assumption of simple "expansion" of the steel bars, due to the positive volumetric difference between corrosion products and iron in metallic state (factor 2 to 6) [1, 17], is based on assuming immediate precipitation of the iron oxides directly at the steel surface. This hypothesis has been confirmed in strongly accelerated corrosion experiments by microscopy analysis of the steel concrete interface, where a thick and dense layer of corrosion products could be found between the steel and the cementitious matrix [5, 6, 10].

In this letter, the approach so far described is analyzed based on electrochemical and physico-chemical considerations, supported by literature evidences. We consider corrosion in carbonated, chloride-free concrete. The influence of chlorides, where iron solubility is increased by the formation of iron-chloride complexes [18] is left for further consideration. Our results show that – in natural, as opposed to accelerated, corrosion conditions – it is unlikely that the primary product of the corrosion redox reaction (Fe^{2+}) reaches saturation. It is suggested that the ferrous ions have the possibility to diffuse into the cementitious matrix before further oxidation and precipitation occurs.

2 Formation of corrosion products

The formation of corrosion products is a necessary step in corrosion induced concrete cracking. In case of chloride contaminated environment the solubility of these products is enhanced by the formation of soluble iron-chloride complexes [18, 19], whereas in carbonated condition it is usually assumed that corrosion products are instantaneously precipitating at the interface [11], due to the low solubility of iron oxides at the pH characteristic of carbonated conditions (pH≈8-9) [20]. In the modeling approaches mentioned earlier, the assumption is that the corrosion rate represents as well the rate of corrosion products formation at the interface (Faraday's law). The basic electrochemical reactions of the steel corrosion process have been described since the beginning of 20th century [21], which also applies to concrete [22]. The steel dissolution process is the transition from metallic state to a bivalent oxidation state of the iron atom (eq. 1):

$$Fe \rightarrow Fe^{2+} + 2e^- \tag{1}$$

However, in studies characterizing the composition of carbonation induced corrosion products formed in concrete, or in other situations such as atmospheric corrosion of steel, the corrosion products have always been found to be composed of compounds with iron in the oxidation state +3 [23-26]. This is because there is an intermediate transformation, that is the spontaneous and fast oxidation reaction of Fe^{2+} ions , which involves oxygen and hydroxyl ions and leads to the final formation of Fe^{3+} (eq. 2) [19, 24].

$$Fe^{2+} \rightarrow Fe^{3+} + e^- \tag{2}$$

While Fe^{3+} oxides and hydroxides are highly insoluble (solubility ≈ 10^{-10} M, depending on pH, Fig. 1) [20, 27] and cause practically instantaneous precipitation upon formation, Fe^{2+} hydroxide ($Fe(OH)_2$) can be significantly more soluble (around 10^{-2} to 10^{-4} M, depending on pH, Fig. 1) [20, 28, 29]. This means that for corrosion products to precipitate, the Fe^{2+} ions released in reaction (eq. 1) must either first be oxidized to Fe^{3+} (eq. 2) (because then the sparingly soluble iron III corrosion products precipitate instantaneously), or the saturation level of Fe^{2+} must be reached in the concrete pore solution (because then iron II corrosion products precipitate). Reaching the Fe^{2+} saturation level in the pore solution is, however, inhibited by i) the oxidation of Fe^{2+} and ii) the continuous transport of Fe^{2+} away from the steel surface. These two processes constantly dilute the Fe^{2+} concentration, at a given, limited rate. However, these two processes are in constant competition with the supply of Fe^{2+} at the steel surface from the anodic iron dissolution reaction (eq. 1). The crucial question to be answered is thus which of the described processes is the fastest. To elucidate this, we present in the next section a numerical model taking into account the described reaction and transport processes.
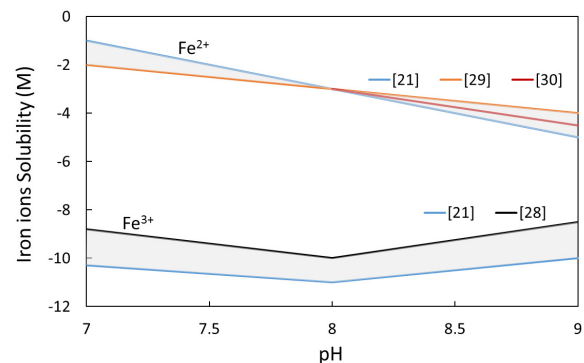

Figure 1. Solubility of Fe^{2+} and Fe^{3+} species in the pH range of carbonated concrete, according to the indicated literature references, illustrating that Fe^{3+} is much less soluble than Fe^{2+}.

3 Modeling transport and precipitation of released iron ions in concrete under natural corrosion conditions

3.1 Description of the model

Here, we propose a model to describe the fate of ferrous ions when released into the concrete during the corrosion process. In this chapter, we consider natural corrosion conditions, that is, corrosion rates that are not accelerated by artificial means (the latter will be addressed in section 5). The following steps are considered in the model, schematically illustrated in Fig. 2:

A. Anodic iron dissolution (eq. 1) leading to release of Fe^{2+} at a given rate. This is the complete corrosion reaction:

$$2Fe + O_2 + 2H_2O \rightarrow 2Fe^{2+} + 4OH^- \tag{3}$$
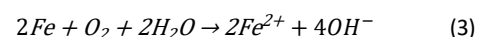
Here we assume the upper range of corrosion rates observed in carbonated concrete, which is $1 \cdot 10^{-6}$ A/cm^2

in water-saturated conditions as was reported in a wide number of studies [30, 31]. The rationale is to consider the most severe iron releasing condition expected in natural (not accelerated) corrosion conditions. In states of lower moisture contents, the corrosion rate can be orders of magnitudes lower, thus the release of Fe^{2+} into the system would be much slower.

B. Direct precipitation of Fe^{2+} according to the reaction

$$Fe^{2+} + 2OH^- \rightarrow Fe(OH)_2 \qquad (4)$$
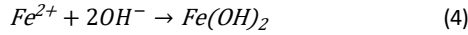
This reaction is assumed to occur immediately (at infinitely high rate) when the saturation level of Fe^{2+} ($1 \cdot 10^{-3}$ M) is overcome.

C. Oxidation of Fe^{2+} to Fe^{3+}. The kinetics of this reaction step is crucial for the model, as the rate at which Fe^{2+} can be oxidized is in competition with the rate at which Fe^{2+} is supplied at the steel surface (anodic dissolution) and the rate at which Fe^{2+} is transported by diffusion. The kinetics of Fe^{2+} oxidation are discussed in more detail below.

D. Precipitation of Fe^{3+}, which is here assumed to occur immediately (at infinitely high rate) when the saturation level of Fe^{3+} is overcome. Note that the solubility of Fe^{3+} oxides is extremely low (ca. $1 \cdot 10^{-10}$ M) [20] (Fig. 1).

E. Transport of Fe^{2+} through the pore system of the concrete. Here, we assume that this transport is governed by diffusion following Fick's laws, and that no significant contribution to the transport comes from migration and convection (see below for a more detailed discussion of these assumptions). Moreover, we assume that the porous system starts immediately from the steel surface, has quasi-infinite length, homogenous porosity and initial concentration of iron ions equal to 0. Further details are discussed below. We acknowledge that the assumption of homogeneity is a strong simplification because it is well known that the steel-concrete interface is not homogeneous, e.g. in terms of porosity [32]. However, we believe that the assumption made here is on the conservative side and is adequate for the illustration of the proposed scientific concept.
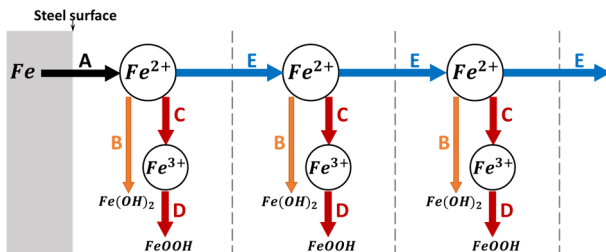

Figure 2. Schematic representation of the model reaction path (steps A to E) from steel corrosion to formation of solid corrosion products in the (water filled) pore system of concrete. The dashed vertical lines represent imaginary vertical slices of the concrete, illustrating the chosen finite element model approach in this work, to predict the concentrations of the different species as a function of both time and distance from the steel surface.

For step (A), given the here assumed corrosion current density of $1 \cdot 10^{-6}$ A/cm^2, it is possible to define the quantity of Fe^{2+} released per unit steel area in 1 second (eq. 3, Fig. 2) as a flux across the steel-concrete interface:

$$J(Fe^{2+}) = 1 \cdot 10^{-7} \, mol/_{s \cdot m^2} \qquad (6)$$

Step (C) describes the oxidation of Fe^{2+} by the aqueous dissolved oxygen, a process that is usually neglected in corrosion induced cracking, but that has also been extensively studied in water research since the early 60s [33, 34]. Reviews of the studies on kinetics of ferrous ions oxidation by O_2 tried to comprehensively merge the knowledge of oxidation kinetics in order to express the process in terms of its controlling parameters, such as pH and forms of Fe^{2+} bearing compounds [28, 35]. Morgan and Lahav [28] showed how, at pH higher than 8 (as in carbonated concrete), the oxidation reaction kinetics are not pH dependent.

Thus, in carbonated concrete, the oxidation (eq. 2) rate can be considered as only dependent on $[Fe^{2+}]$ and amount of dissolved oxygen $[O_2]_{aq}$ (eq. 7).

$$\frac{-d[Fe^{2+}]}{dt} = k[Fe^{2+}][O_2]_{aq} \qquad (7)$$

With k kinetic constant, which over the years has been studied, resulting in values spanning over two orders of magnitude (from 15 s$^{-1} \cdot$M^{-1} [35] to 400 s$^{-1} \cdot$M^{-1} [28], calculated as per constant O_2 partial pressure, 0.2 bar). The pH was assumed constant over the entire simulation domain, as it would be buffered by the cement pore solution chemistry. Typical pH range for carbonated concrete is from 7.2 [36] to 9.5 [37], in this case the pH was assumed to be 8 (Fe^{2+} solubility, $1 \cdot 10^{-3}$ M). The kinetic constant of the ferrous iron oxidation reaction (k, eq. 7) has been varied around the interval found in literature (2.5, 15 and 100 s$^{-1} \cdot$M^{-1}).

Step (E) describes the transport of Fe^{2+} ions by diffusion. No reliable studies are available for the diffusion properties of Fe^{2+} in concrete at the best of our knowledge. Thus, we will here take the diffusion coefficient of chlorides (Cl$^-$) as reference, as the transport properties of chloride ions in concrete are intensively studied. The intrinsic diffusion coefficient of Cl$^-$ in water is ca. $1 \cdot 10^{-5}$ cm^2/s, while in concrete the Cl$^-$ effective diffusion coefficient (D_{eff}) has been measured to be between ca. $1 \cdot 10^{-8}$ cm^2/s and $2 \cdot 10^{-7}$ cm^2/s [38-41]. The same proportionality has been assumed to hold for Fe^{2+}. Starting from its intrinsic diffusion coefficient in water ($7 \cdot 10^{-6}$ cm^2/s), the Fe^{2+} effective diffusion coefficient in concrete has been assumed as $1 \cdot 10^{-7}$ cm^2/s, applying the same proportionality. In the model, the Fe^{2+} effective diffusion coefficient was varied ($1 \cdot 10^{-6}$, $1 \cdot 10^{-7}$ and $1 \cdot 10^{-8}$ cm^2/s) in order to assess its influence on the species concentration and to simulate the possible effect of a denser or more open pore structure.

Liquid advection is not considered in this model, since moisture saturated condition is assumed in this study. Migration of ions as an additional transport mechanism is not included in the model based on the assumption that the ionic strength of pore solution in a carbonated system is still

relatively high [36], thus even Fe^{2+} concentration at saturation level ($1 \cdot 10^{-3}$ M) can be considered negligible in terms of ionic strength. The authors of this letter extracted pore solution from four different fully carbonated samples (Table 1). The extraction has been performed by means of an hydraulic press, applying a pressure up to 300 MPa for a time comprised between 30 minutes and 3 hours. The data agrees with what was found in literature [36] and the ionic strength is about 100 times higher compared to Fe^{2+} saturation ($1 \cdot 10^{-3}$ M) (Table 1).

Table 1. Composition of pore solution extracted from fully carbonated (4% CO_2) and water saturated samples obtained from ICP analysis.

Mix	Ca (g/l)	K (g/l)	Na (g/l)	S (g/l)	Ionic strength (M)
CEM I, 0.5	0.744	0.590	0.128	0.624	0.086
CEM I, 0.6	0.742	0.580	0.126	0.700	0.091
CEM II, 0.5	0.754	0.654	0.186	0.636	0.090
CEM II, 0.6	0.698	0.656	0.332	0.792	0.100

In summary, the present model considers the following species: Fe^{2+}; $Fe(OH)_2$; $FeOOH$; O_2.

To solve the above described diffusion-reaction problem, a 1D finite element model with two modules – diffusion and chemical reaction – was implemented in COMSOL Multiphysics. The model setup is based on the schematic drawing in Fig. 2, as Fe^{2+} is released from the rebar on the left and directly diffuses into concrete perpendicular to the rebar surface. The length of the simulation domain is 2 mm which is clearly longer than the corrosion products penetration depth generally observed in the literature in case of chloride-free conditions (e.g., Fig. 6).

3.2 Modeling results

The simulations show that the stationary state of concentrations of dissolved species is achieved within few hours, even at a distance of 1 mm from the steel surface (Fig. 3). Thus, to illustrate the spatial distribution of Fe^{2+} in the pore solution of the concrete, Figs. 4 and 5 detail model results obtained at t = 50 h. The differences between the plots shown in Figs. 4 and 5 can be found in different combinations of assumed Fe^{2+} oxidation kinetics (k) and ferrous ion diffusion coefficients (D_{eff}). This permits to analyze the competition between the different processes shown in Fig. 2, namely release (step A), oxidation (step C), and diffusive transport (step E) of Fe^{2+}.

As expected, the concentration of Fe^{2+} at the steel surface is depressed if both oxidation and diffusion are fast. It is one of the key results of this study that even for a fast corrosion rate (the here assumed rate represents the upper range of what can be expected under natural, non-accelerated conditions) the solubility threshold of Fe^{2+} is never reached, which means that there is no formation of solid Fe^{2+} corrosion products ($Fe(OH)_2$). While the Fe^{2+} concentration at the steel surface varies between $1 \cdot 10^{-5}$ and $1 \cdot 10^{-4}$ M, depending on the assumed k and D_{eff}, even the assumption

of slow oxidation kinetics and low ferrous ion diffusion coefficient, within the range of what can reasonably be expected in concrete, will lead to Fe^{2+} concentrations approx. one order of magnitude lower than the solubility threshold (Figs. 4 and 5).

Concerning the spatial distribution of ferrous ion in the concrete, the model confirms the expectations that i) fast oxidation kinetics depress the Fe^{2+} concentration everywhere in the concrete (because this is a general sink term), and ii) fast diffusion shifts the Fe^{2+} to larger distances from the steel surface. The distribution of relevant Fe^{2+} ion concentrations spans over a range of up to hundreds of microns, depending on the input parameters, therefore the region of interest is not restricted to the steel surface zone (Fig. 3 to 5). From the here presented simulation, it can be seen that, using an intermediate kinetic constant k (15 $M^{-1} \cdot s^{-1}$) and D_{eff} ($1 \cdot 10^{-7}$ cm^2/s), ca. 20% of the Fe^{2+} present at the steel surface is able to diffuse over 10 µm (Fig. 3) and ca. 1% of the Fe^{2+} ions, is even able to reach 100 µm distance (Fig. 3), while only about 0.01% can reach 1 mm. If the oxidation kinetics are reduced from k=100 $M^{-1} \cdot s^{-1}$ to k=2.5 $M^{-1} \cdot s^{-1}$ the concentration of Fe^{2+} at 100 µm increases almost 40 times (Fig. 3 and 4a). While, considering different diffusion properties, when D_{eff} is increased from $1 \cdot 10^{-8}$ cm^2/s to $1 \cdot 10^{-6}$ cm^2/s, the amount of Fe^{2+} ions able to reach 100 µm increases by a factor ca. 60 (Fig. 4b). In the extreme cases, when slow oxidation (k=2.5 $M^{-1} \cdot s^{-1}$) and fast diffusion (D_{eff}=$1 \cdot 10^{-6}$ cm^2/s) case is compared to fast oxidation (k=100 $M^{-1} \cdot s^{-1}$) and slow diffusion (D_{eff}=$1 \cdot 10^{-8}$ cm^2/s), the Fe^{2+} concentration at 100 µm increases of a factor 10^3 (Fig. 5).

3.3 Considerations on the modeling results

The proposed model is based on literature data and a number of assumptions. These are:

- Chloride-free, carbonated cementitious matrix;
- Only transport by diffusion is considered;
- Matrix porosity is considered constant from the steel surface into the porous system bulk;
- Precipitation is considered instantaneous when saturation is reached.

The simulations results are supported by experimental findings, as will be shown in the following section. It is worth pointing out that in the present model the corrosion rate is taken into account at its highest value expected in natural corrosion conditions, therefore when precipitation and accumulation at the steel-concrete interface would be the highest. However such situation can only occur in exposure class XC4 (according to European standard EN 206-1) and even then represents only a very limited part of a structure's life time, over which it is much more common to have (extended) periods of lower corrosion rates (due to seasonal exposure climate variations). For a lower corrosion rate, the ferrous ions would have even more time for diffusion and oxidation [17].
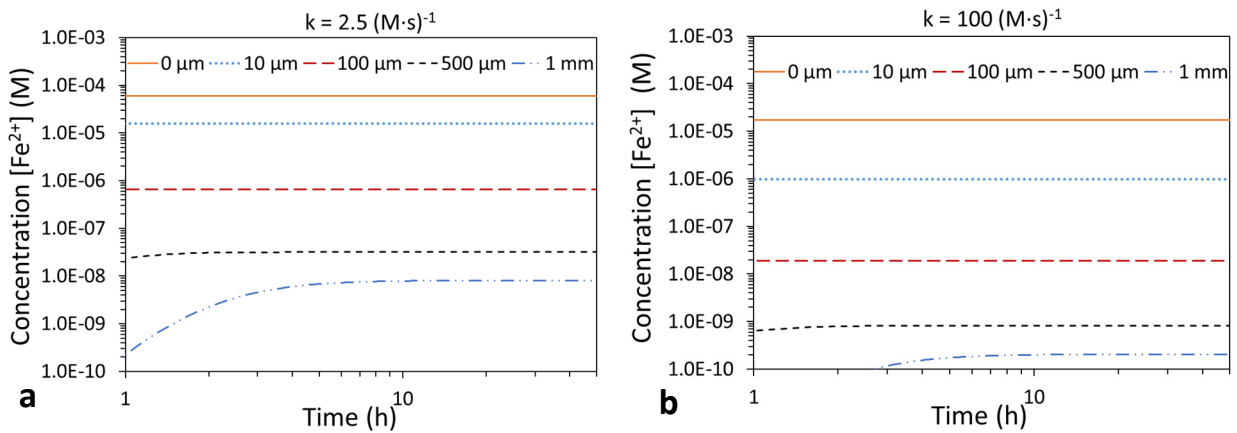
Figure 3. Concentration of Fe^{2+} over time, at different distances from the steel surface (0, 10, 100, 500 µm and 1 mm). Process modeled for D_{eff} = $1 \cdot 10^{-7}$ cm²/s and different oxidation kinetic constants (eq. 7): a) k= 2.5 1/(M·s) (slow), b) k= 100 1/(M·s) (fast). The figures show that after 10h the concentration of Fe^{2+} has achieved the steady state for all considered distances. Also, the results show that a higher Fe^{2+} oxidation rate leads to a lower concentration of Fe^{2+} at all depths.
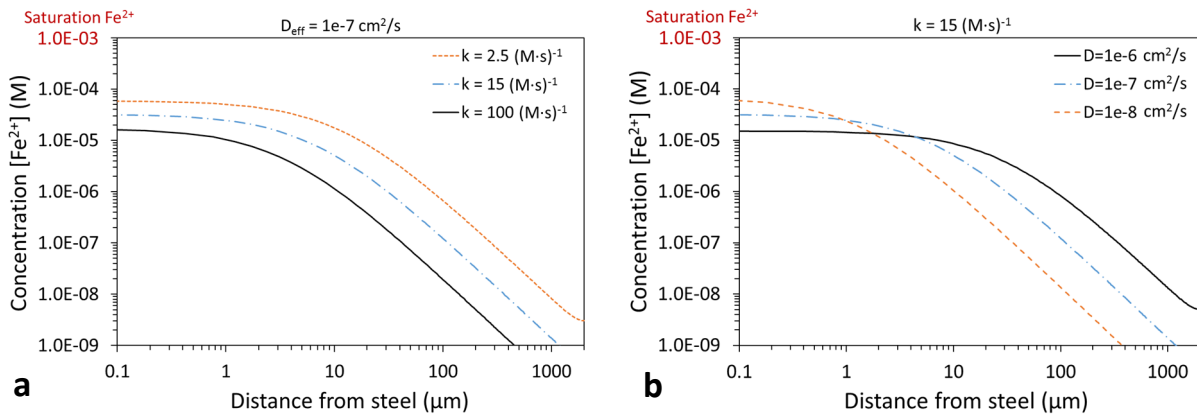

Figure 4. Concentration of dissolved Fe^{2+} in case different oxidation kinetic constants are used at fixed D_{eff} ($1 \cdot 10^{-7}$ cm²/s, intermediate diffusion coefficient) (a) and if different effective diffusion coefficients are used at fixed k (15 $M^{-1} \cdot s^{-1}$, intermediate oxidation rate) (b) as a function of the distance from the steel surface (at t=50 h). As expected, the concentration of Fe^{2+} at the steel surface increases if the Fe^{2+} sinks, namely Fe^{2+} oxidation and Fe^{2+} diffusion, are slow. Nevertheless, in all here studied combinations, the Fe^{2+} concentration at the steel surface is always lower than the saturation threshold, thus, no Fe^{2+} precipitation is expected to occur.
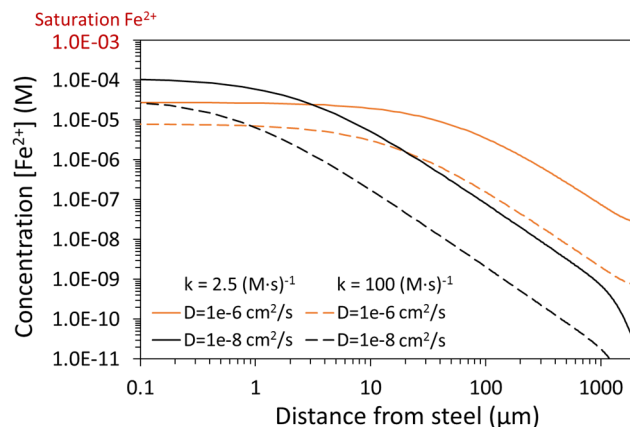

Figure 5. Concentration of dissolved Fe^{2+} as a function of the distance from the steel surface (at t=50 h) in the extreme combinations of slow and fast rates of oxidation and diffusion, respectively. The Fe^{2+} concentration distant from the steel surface is strongly influenced by these parameters, while the concentration at the steel surface only varies over 1 order of magnitude. It is important to note, however, that even for the combination of slow Fe^{2+} oxidation and slow Fe^{2+} diffusion, the Fe^{2+} concentration never reaches the saturation level (still ca. 1 order of magnitude lower), thus, no Fe^{2+} precipitation is expected to occur.

In engineering structures, the situation of multilayer rebars may lead to a macro-cell corrosion mechanism also for carbonation induced corrosion [42]. In this case the actual corrosion rate of the active areas can be increased, by the presence of the nearby passive rebar layers (in uncarbonated concrete). Due to area effects, however, the increase of corrosion rates compared to situations without additional cathodic rebar layers will be limited to a factor around 2-3 [42]. However, in view of the described model, this would primarily affect the input corrosion rate value; whereas the reaction and diffusion kinetics of Fe^{2+} would not be substantially affected, as they are only dependent on the pore solution pH and composition (chloride-free and pH 8, in the present model) and on the transport properties (function of porosity). In fact, this model merely describes the reactive transport mechanism of Fe^{2+} released upon corrosion, regardless of the corrosion mechanism, this being either natural, macro-cell or artificially accelerated corrosion; provided the chloride-free condition is satisfied.

Finally, as mentioned, the actual concentration of Fe^{2+} at the steel surface appeared to be always clearly lower than the saturation threshold, but also higher than $1 \cdot 10^{-6}$ M. The latter is a common assumption made, e.g. in standard representations of the Pourbaix diagram of iron [43]. The actual concentration of Fe^{2+} at the steel surface depends on the Fe^{2+} oxidation rate and on the effective Fe^{2+} diffusion coefficient (function of the pore structure [44, 45]), and on the corrosion rate. It is important to recognize, that the concentration of Fe^{2+} at the steel surface is not a constant, but, depending on the system and on the exposure conditions, may vary over a range of approx. 1 order of magnitude – or even more (Fig. 3-5 did not show the results for lower corrosion rates, where, however, the Fe^{2+} concentration can be even lower). This has major implications for the electrochemistry of steel in concrete, because the concentration of Fe^{2+} at the steel surface directly affects the reversible potential (E_a) of the anodic reaction (eq. 1) described by the Nernst equation:

$$E_a = E_{Fe/Fe^{2+}}^{rev} = E_{Fe/Fe^{2+}}^0 + \frac{RT}{nF} \ln Fe^{2+} \qquad (8)$$

Here, $E_{Fe,Fe^{2+}}^0$ is the standard potential, n is the number of electrons exchanged, F the Faraday constant, R the gas constant, and T the temperature. A lower Fe^{2+} concentration depresses the reversible potential of the Fe/Fe^{2+} electrode, which leads to an increase in the corrosion current density, as based on well-established considerations regarding corrosion kinetics [1]. It is beyond the scope of this letter to discuss the consequences of this in detail.

4 Observations of distribution of corrosion products under natural corrosion conditions

This section presents experimental evidences that products of carbonation-induced corrosion can travel far from the steel surface.

In the PhD thesis of Constantinou, microstructural analysis showed the distribution of corrosion products around the steel rebar [46] when the corrosion process occurred in natural exposure conditions, that is, without any acceleration of the corrosion process. According to these findings, the corrosion products could penetrate to distances up to the millimeter scale, without causing any concrete cracking.

Experiments carried out by the authors of this letter showed similar results. Thin carbonated mortar samples [47, 48], reinforced with steel wires, were exposed to different humidity environments where corrosion occurred naturally. Corrosion rates were in the range $1\text{-}4\cdot10^{-7}$ A/cm^2. After about one year, sections perpendicular to the steel wires, of samples exposed to 99% RH, were cut, polished and analyzed by SEM/EDX, in order to map the distribution of corrosion products. Fig. 5 shows an example of these analyses, showing how, in one year, the corrosion products spread to depths up to 0.5 mm within the mortar pore structure. It can be noticed how the products traveled around the aggregates of the mortar. It may be worth mentioning that the mortar was found uncracked at the time of terminating the corrosion experiments.

Unfortunately, such studies are rare in literature, especially in the context of carbonation-induced corrosion. Nevertheless, the experimental findings – both those reported by Constantinou [46] and the authors of this letter – support the modeling results, as they show how the precipitation of iron oxides can happen deep into the pore structure after Fe^{2+} formation at the steel surface.
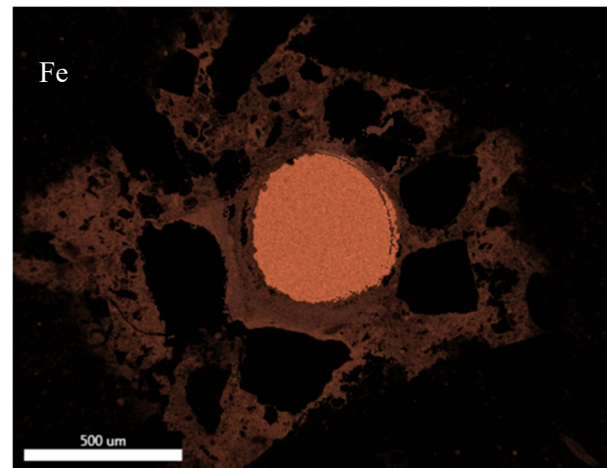

Figure 6. Iron mapping by SEM/EDX samples of a cut section of steel wire (diameter 0.5mm) embedded in a carbonated mortar (binder CEM II/B-M (T-LL), w/b ratio 0.6) and exposed to 99% RH for 1 year.

5 Implications for accelerated corrosion testing

Common experiments of corrosion-induced cracking, against which concrete-cracking models are calibrated, typically make use of corrosion accelerating techniques (e.g. impressed current methods). Corrosion rates are often significantly accelerated – 10 to 1000 times higher than the natural process [5-10] – which leads to a very fast release of Fe^{2+} at the steel surface. The impact of this on corrosion products formation can be illustrated with help of the model presented in this work.

Considering a corrosion rate 100 times higher than $1 \cdot 10^{-6}$ A/cm^2 (the latter represent an extreme case under natural conditions), the ferrous ions produced by the process also are (eq. 9).

$$J(Fe^{2+}) = 10^{-5} \, \frac{mol}{s \cdot m^2} \qquad (9)$$

By keeping all other model inputs identical with what was presented in section 3, the results shown in Fig. 7 are obtained. The Fe^{2+} concentration at the steel surface is now much higher than in conditions of natural corrosion (Figs. 4-5). In fact, the saturation level is now overcome, due to the accelerated corrosion process, causing, as a consequence, precipitation of the released ferrous ions at the steel-concrete interface directly in the form of Fe^{2+} rust. Further precipitation of Fe^{3+} products occurs at the highest possible rate (proportional to [Fe^{2+}], eq.7). Fig. 7 does not show that the concentration of Fe^{2+} in accelerated corrosion condition exceeds saturation because, as by step B of the modeling (Fig. 2), Fe^{2+} is assumed to precipitate as soon as the saturation threshold is reached. Therefore the simulation cannot show a Fe^{2+} concentration as high as the saturation level. However, from the calculated formed Fe(OH)$_2$ it becomes clear that Fe^{2+} precipitates under accelerated conditions (Fig. 7).

The formation of solid Fe(OH)$_2$ (and FeOOH) can block pores and thus further reduce the penetration of Fe^{2+} into the concrete matrix [10]. This was not considered in our model, but is expected to increase the Fe^{2+} concentration at the steel surface even more (leading to even more precipitation).
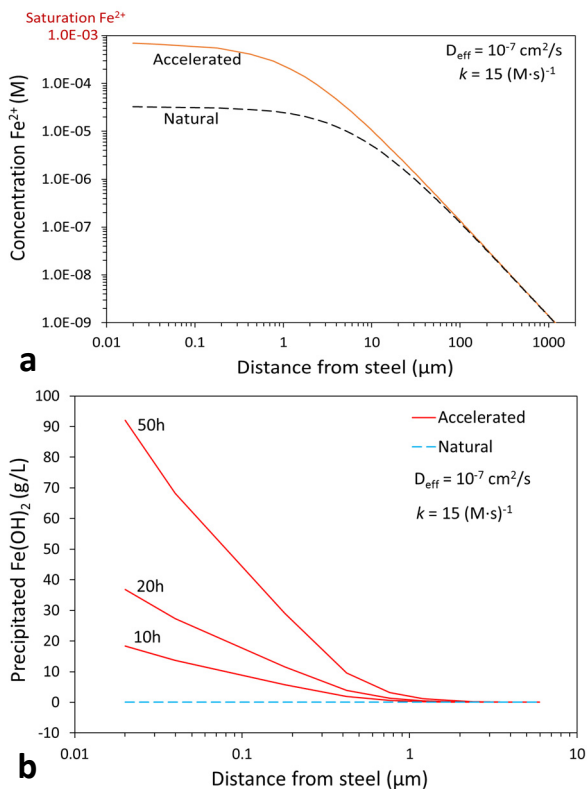
Figure 7. (a) Fe^{2+} concentration at the steady state, in case of accelerated corrosion testing in comparison with natural corrosion conditions. The accelerated process causes more than one order of

magnitude higher Fe^{2+} concentration, at the steel surface, than what would occur in natural conditions, and leads to the precipitation of Fe(OH)$_2$ and its accumulation over time, which would not occur in natural conditions (b).

6 Conclusions

This letter presented a conceptual model describing the fate of ferrous ions released during corrosion at the steel surface. The concentration of Fe^{2+} ions in the concrete pore solution is the result of a competition between the following processes: supply (anodic iron dissolution at the steel surface), oxidation, and transport of Fe^{2+}. Depending on the actual conditions, the concentration of Fe^{2+} may or may not reach the saturation threshold, thus Fe(OH)$_2$ may or may not precipitate. On the basis of numerical simulations and experimental results, the following major conclusions can be drawn:

- Under natural corrosion conditions, the saturation of Fe^{2+} is unlikely reached. This means that Fe^{2+} ions remain in dissolved state and may diffuse over considerable distances before being oxidized, in presence of oxygen, to Fe^{3+}, in the form of which they precipitate.

- Under accelerated corrosion conditions (e.g. impressed anodic currents), the saturation of Fe^{2+} is likely exceeded at the steel surface. This means that Fe^{2+} immediately precipitates as Fe(OH)$_2$, which prohibits further transport away from the steel surface.

- The distance to which corrosion products can diffuse under natural corrosion conditions before precipitating can be of the order of several 100 microns to millimeters. Thus, the pore volume being gradually filled with corrosion products can be considerably larger than in accelerated corrosion situations.

- As a consequence, expansive stresses giving rise to cracking can be reached at lower steel sectional area losses under accelerated test conditions, than under natural corrosion conditions.

- Models to predict corrosion-induced cracking may benefit from taking into account the Fe^{2+} reactive diffusion process here described. Such future research work would need to study in more detail the transport properties of ferrous ions in concrete, the impact of the microstructure at the steel-concrete interface, etc.

- Finally, the concentration of Fe^{2+} ions at the steel surface can vary over at least one order of magnitude, which has an influence on the electrochemistry of steel in concrete, ultimately affecting the corrosion kinetics. This could also be taken into account in mechanistic models for the corrosion rate in concrete.

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